A Compositional Petri Nets Semantics for Basic LOTOS

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Abstract: In this study, we propose a formal semantics for Basic LOTOS Language Of Temporal Ordering Specification). This is the subset of LOTOS where processes interact with each other by pure synchronizations, without exchanging values. In basic LOTOS we can appreciate the expressiveness of all the LOTOS process constructors (operators) without being distracted by interprocess value communication. LOTOS is an FDT generally applicable to distributed, concurrent information processing systems. During the last decade, a lot of works have been devoted to compilation and verification of LOTOS specifications. While using extended Petri nets as tool for compile a subset of LOTOS has already been pointed out. In this article we propose to extensively make use of a specific kind of high level Petri nets: the M-nets. Such nets, allowing for compositionality, appear particularly well-suited to give a formal semantics for basic LOTOS.

Key words: Specification, Petri nets, M-nets, compositionality, semantics, LOTOS

INTRODUCTION

LOTOS (Bolognesi and Brinksma, 1987) is one of the Formal Description Techniques FDT developed within ISO for the formal specification of open distributed systems. In LOTOS a distributed, concurrent system is seen as a process, possibly consisting of several subprocesses. A LOTOS specification describes a system via a hierarchy of process definitions. A process is an entity able to perform internal, unobservable actions and to interact with other processes, which form its environment.

Basic LOTOS is a simplified version of the language employing a finite alphabet of observable actions. This is so because observable actions in basic LOTOS are identified only by the name of the gate where they are offered and LOTOS specifications can only have a finite number of gates.

The M-nets Calculus (Best et al., 1995, 1999, Hugon, 1996), defined as the high level or coloured version of the Petri Box Calculus (PBC) (Best et al., 1992), is widely accepted to give semantics to concurrent systems and programming languages like B(PN)\textsuperscript{2} and SDL, cf. (Lilus and Pelz, 1996; Fleis Chlack and Grahmann, 1997; Klaudel and Riemann, 1998; Hugon, 1996; Benzaïken et al., 1998). The most original aspect of M-nets is their full compositionality thanks to their interfaces and a set of various net operations defined semantics for them. In fact, M-nets constitute like PBC a net algebra. Their interest is augmented by the ability to use in practice an associated tool PEP (Programming Environment based on Petri nets) (Grahmann, 1997), which also offers various implemented verification and analysis methods. Whenever the system to be modeled consists of a lot of distinct conceptual parts, which need to be combined or coordinated in a nontrivial way, a very modular and compositional proceeding is necessary to be able to control the correctness of modeling M-nets just offer these features.

We have chosen to translate basic LOTOS specifications into the algebra of modular high-level Petri nets: the M-nets (Best et al., 1995, 1999, Klaudel, 1995). Due to the rich set of composition and communication operators we are able to define a semantic operator on M-nets for each syntactic operator of basic LOTOS.

Using our approach a property of a basic LOTOS specification is checked as follows:

- The M-net semantics of the basic LOTOS specification is calculated.
- The M-net is unfolded into a Petri box (a special low-level net) (Best et al., 1992).
- The basic LOTOS property is transformed into a net property.
- The net property is checked against the Petri box.
- The result is transformed back to the basic LOTOS level.

BASIC LOTOS SPECIFICATION

Systems and their components are represented in LOTOS by processes. A specification is the process that represents the whole system being specified. A process displays an observable behavior to its environment in terms of permitted sequences of observable actions. A process appears as a black box to its environment since
the environment has no information about its internal structure and mechanisms. Processes may have a local definitions (after the keyword where) in which other processes can be defined.

LOTOS has scoping rules similar to block-structured programming language. The structure of basic LOTOS specification is:

```
specification spec-name [gate list]; functionality
where
  [process definitions]
endspec
```

where gate list is a finite alphabet of gate names (or observable actions). A behaviour expression is built by applying an operator (e.g., [ ] to other behaviour expressions. A behaviour expression may also include instantiations of other processes whose definitions are provided in the where clause following the expression.

The complete list of basic LOTOS behaviour expressions is given in Table 1, which includes all basic LOTOS operators.

Symbols $B_1, B_2, B_3$ stand any behaviour expression; $G, G_1, G_2, \ldots, G_n$ are elements of a finite alphabet gate list.

**Remark:** The parallel operator || take an important part in the M-nets algebra; thus, in order to avoid confusion we reserve this notation for the composition of M-nets. In the sequel, for LOTOS, the notation for the operator of full synchronization will be $[G']$ instead of || where $G'$ is the set of all gates which are defined in both behaviours or both processes.

**M-NETS**

The M-nets algebra was introduced by Best et al. (1995, 1999) as an abstract and flexible metalanguage for the definition of semantics of concurrent programming languages. These allow (as usually composition operators in process algebras do) the compositional construction of complex nets from simple ones, thereby satisfying various algebraic properties.

The main difference between M-nets and coloured nets is that M-nets carry additional information on their places and transitions to support composition operations. Besides annotations on places (set of allowed tokens), arcs (multisets of variables and transitions (occurrence conditions), M-nets have, additionally, labels on places and labels on transitions. The labels on transitions denote communication capabilities similar to action symbols in a CCS term, respectively indicate their hierarchical nature. The labels on places denote their status as entry (part of the initial marking), exit (part of the final marking) or internal (otherwise). Thus, every place and transition of an M-net carries an inscription of the form inscription = (label | annotation).

**Auxiliary definitions:** Let Val be a fixed and suitably large set of values, Var, resp. X sets of variables, resp. hierarchical variables, the latter ones being capital letters and Par a set of parameters.

We assume the existence of a fixed but sufficiently large set $A$ of parametrised action symbols. Each action $A \in A$ is assumed to have an arity $\text{ar}(A)$ which is a natural number describing the number of its parameters. The elements of $A$ are grouped into pairwise conjugates by the bijections $A \rightarrow A$, called conjugation, satisfying: $\forall A \in A : A \neq A$, $A$ and $\text{ar}(A) = \text{ar}(A)$

We also assume the existence of a fixed but sufficiently large set $G$ of action gate symbols without conjugation. Each action gate symbol $G \in G$ is assumed to have an arbitrary arity $\text{ar}(G)$. An action term is, by definition, a construct $A_{\tau_1 \ldots \tau_{\pi_0}}[G_{\pi_1 \ldots G_{\pi_k}}]$ where $A \in A$ and $\tau_i \in \text{Var} \cup \text{Val}$ for $1 \leq i \leq \text{ar}(A)$, $G \in G$ and $G_i \in$ gate list for $1 \leq i \leq \text{ar}(G)$.

**Definition of M-nets:** An M-net is a triple $(P, T, \lambda)$ such that $P$ is a set of places, $T$ a set of transitions with $P \cap T = \emptyset$, $\lambda$ is an inscription function with domain $P \cup (P \times T) \cup T \times P \cup T$, such that:

- For every place $p \in P$, $\lambda(p)(\alpha_\lambda, \beta_\lambda)$, where $\alpha(p) \in \{a, I, x\}$ is called the label or status of $p$ and $\beta(p)$, the type of $p$, is a nonempty set of values from $\text{Val}$.
- For every transition $t \in T$, $\lambda(t)$ is a pair $\langle a_\lambda, b_\lambda \rangle$ where $a_\lambda$ is the label of $t$, is a finite multiset of action terms (it will then be called a communication transition), or a hierarchical action symbol, i.e., $a_\lambda(t) \in X$, (it will then be called a hierarchical transition); $b_\lambda(t)$, the guard of $t$, is a multiset of terms over $\text{Val}$ and $\text{Var}$.
- For every arc $(p, t) \in (P \times T)$, $\lambda(p, t)$ is a finite multiset of variables from $\text{Var}$ and values respecting the type of the adjacent place $p$, (analogous for arcs $(t, p) \in (T \times P)$, the meaning of $\lambda(p, t) = \emptyset$ is that there is no arrow leading from $p$ to $t$.

**Operations on M-nets:** The composition operators on M-nets as defined by Best et al. (1995), Klaudel (1995) are two different kinds: those concerning place interfaces and thus the flow control (which comprise sequential composition $\cdot'$, choice $\cdot$), parallel composition $||$ and iteration $^*$ and those concerning transition interfaces and thus capabilities for communication comprising synchronization and restriction.
The intuitive idea behind the synchronisation operation of an M-net N consists of a conglomeration of certain basic synchronisations over actions terms pairs (A, ...) and A (...,) and yield a new transitions in N (Best et al., 1999). The operation will be defined as follows: N sy A, where N = (P, T, λ) is a given M-net and A is a given action symbol. The communication is performed by a most general unifier which renames the variables in the action terms appropriately (Klaadal, 1995).

The restriction operation N rs A removes from N all transitions that mention either A or A and hence all synchronisation capabilities for A. Scoping is a mixed operation, accepting an M-net and a set of communication action symbols; it is defined by the synchronisation followed by the restriction of the net over the set of action symbols: N' = (N sy A) rs A. This scoping mechanism is used for block structuring.

**M-net model extensions:** In order to adapt the M-net model for a basic LOTOS compositional semantics, the operations on M-nets must be extended to some other operators such that:

- The M-net refinement (Devi lers et al., 1997, 1999; Klaadal and Riemann, 1998): N (X < - N[i = f]) allowing a hierarchical construction of M-net, means N where all X-labelled (hierarchical) ! transitions are refined into (i.e., replaced by a copy of) N[i, for each i in the indexing set I.

However, general refinement (Devi lers et al., 1997) is not sufficient for our approach, in fact, knowing that a LOTOS system is described via a hierarchy of process definitions we must have a possibility to distinguish different instantiations of a process definitions and their behaviours. In order to satisfy this requirement, we use the general parametrised refinement concept (Dev lers et al., 1997). The parameter mechanism is the mean by which a refining net interact with the area of the refined transition.

In this way, we add a formal parameter to hierarchical transition which deals with the concrete parameters of the call and return transitions labels.

- The synchronization-lotos (Mekki, 2000) sy is defined such that:

Let two M-nets N_i = (P_i, T_i, λ_i) and N_j = (P_j, T_j, λ_j) and let G an action gate symbol.

\( (N_i \parallel N_j) \text{ sy}_G \) where: \( \delta = P_i \cup P_j \cup T = T_i \cup T_j \cup T_{\text{y}}(T_{\text{y}} \cup T_{\text{y}}) \) where \( T_{\text{y}} \) is the set of transitions \( t_y \) arising through a basic synchronisation-lotos out of \( t_i \) and \( t_j \) over G such that:

\[ t \in T_{\text{y}}, t_i \in T_{\text{y}} \text{ and } T_{\text{y}} = T_i \cup T_{\text{y}} = T_j \cup T_{\text{y}} \]

\[ \lambda = (\lambda_i \cup \lambda_j) \text{ sy}_G \] where \( \alpha (t_i) = \alpha (t_j) = \alpha (t) \).

- The relabelling function (Mekki, 2000): \( \Pi_{\text{sy}_G} \) which is applied to an M-net N, is parametrised with a name of process definition (P) and a list of gate names (gate-list). It does the following substitution for each gate name \( G_i \in \text{gate-list} \) in N.

**SEMANTICS OF A BASIC LOTOS SPECIFICATION**

A semantics of basic LOTOS specification will be defined associating one M-net to:

- Each process definition (avowed in the where clause)
- Its behaviour expression
- The initialization and clearing of each process definition

The M-net of the last two kinds have to be composed sequentially with each other to enable later scoping over (created and terminated) processes. Finally, all these M-nets are put in parallel and

- The synchronization and restriction over all action names in the process definitions will insure the scoping. Thus, we get above global semantic formula:

\[ M \text{ - net}(\text{blok}) = [M \text{ - net(process definitions)}] \parallel [\big( \Pi_{\text{sy}_G} \text{ (processes)} \big)] \]  

\[ \Pi_{\text{sy}_G} \text{ (processes)} \text{ rs } \Pi_{\text{sy}_G} \text{ (processes)} \]

With

\[ \Pi_{\text{sy}_G} \text{ (processes)} = \big| \sum_{i \leq n} \gamma_{t_i} \text{ (process)} \big| \]

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Where, \( \gamma_{t_i} \) (process) \( \gamma_{t_i} \) are the auxiliary M-nets for initialization and termination of scoping.

In the sequel, the other M-nets appearing in the above global semantic formula will be precisely defined as well as the considered sets of action symbols.

**Semantics of process definition:** A process definition is similar to a procedure declaration in a programming language like Pascal.
Let us first examine a single instantiation of a process. It is easy that it consists of a call transition, a return transition and a body. The call transition is labelled \( p \) with while the return transition is then correspondingly labeled with \( p \). The control flow in the body is represented by the block to which moves through the body representing the different actions that the process executes. The call of the process is equivalent to the synchronisation with \( p \), of the M-net for instantiation (Fig. 4). However if several instantiations of the process are active at the same time, this simple scheme does not work. The reason for this is, that since the control tokens have no identity, we may not distinguish between them and so the causal relations between the control and the process instantiations may be broken.

We propose to solve the problem by using colored tokens \((id)^\) as indexes to distinguish between the instantiations, allowing to fold the different instantiations of the process into one M-net.

Thus in the M-net construction of process definition semantics (Fig. 1), we allow \( Id(p) \) (the instantiation set) as type for internal places and \( id \) as concrete parameter for actions of hierarchical transition \( t \).

In the sequel we suppose that the set \( Id(P) \subseteq \text{Val} \) of instantiation identifiers is given.

Generally a specification LOTOS is a hierarchy of processes. Therefore, we may have overlapping process definitions. Hence, in order to deal with process definition formally, we will denote by \( P_i \) a process definition identifier at the jth level of overlap (with \( 1 \leq j \leq m \) where \( m \) is the maximal depth of overlap).

The box M-net (procd of) of a process definition declared at the level of overlap depth \( j \) is obtained by successive refinements in the operator M-net \( N_i \): \( id_i \): \( Id(P) \),..., \( id_i \): \( Id(P) \) of semantic components of \( P_i \) where:

\[ N_i: id_i: Id(P),..., id_i: Id(P) \]

In charge for the management of instantiations \( P_i \);

\( N_i \) (id: Id(P) in charge for the initialization (call) and the termination (return) of each instantiation of \( P_i \);

In the box \( N_i \) (id: Id(P), the transition labelled \( \gamma_i \) is a hierarchical transition which is refined by the representative net of process definition body: \( N_i \) (id). The event of the transition \( t_i \) carried out by synchronization with the transition labelled by its complementary action belonging to the instantiation M-net (that we will see further) of the process according to the behaviour expression of the block; thus the list of the formal gates \( gate list \) in the net

\[ N_i (id: Id(P))(\gamma_i (id_i) \gets N_i (id_i)) \]

Table 1: Syntax of behaviour expressions in basic LOTOS

<table>
<thead>
<tr>
<th>Syntax</th>
<th>Non-phonetic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inaction</td>
<td>Stop</td>
</tr>
<tr>
<td>Termination+</td>
<td>End</td>
</tr>
<tr>
<td>Prefixage</td>
<td>iB</td>
</tr>
<tr>
<td>Action</td>
<td>G:B</td>
</tr>
<tr>
<td>Choice</td>
<td>B_i \cup B_j</td>
</tr>
<tr>
<td>Composition</td>
<td>B_i \cup G_i</td>
</tr>
<tr>
<td>Casemake</td>
<td>B_i \cup B_j</td>
</tr>
<tr>
<td>Synchronisation</td>
<td>B_i \cup B_j</td>
</tr>
<tr>
<td>Abstraction</td>
<td>B_i \cup G_i</td>
</tr>
<tr>
<td>Composition</td>
<td>B_i \cup B_j</td>
</tr>
<tr>
<td>Preemption</td>
<td>B_i \cup B_j</td>
</tr>
</tbody>
</table>

must be renamed in list of effective gates belonging instantiation Pcall M-net.

Finally, after refinement in \( N_i (id: Id(P)) \) we obtain:

\[ N_i (id: Id(P)) = N_i (id: Id(P)) \]

\[ [\gamma_i (id_i) \gets N_i (id_i)]P_i \]

M-net (procd of) \( P_i \) (gate list) =

\[ N_i (id: Id(P),..., id_i: Id(P)) \]

\[ [R_i \gets N_i (id: Id(P))]P_i \]

In a basic LOTOS specification or process, the declaration semantics of many process definitions with same overlap level is given by the following formula:

M-net (process definitions) = \( \prod \Gamma_i \)

and the action symbols for scoping are:

\[ \Gamma (process) = \sum \gamma_i (process) \]

where:

\[ \gamma_i (process) = \{ p\_n, p\_r, p\_init, p\_term, p\_external \} \]

with

\[ \text{ar}(p\_n) = 1 \]

and

\[ \text{ar}(p\_init) = 0 \]

Behavior expression M-net: An essential component of a specification is its behaviour expression where the observable and internbehaviours are defined.
In the sequel, the M-nets semantics of each operator (Table 1) is given.

Inaction specified by stop, models a situation in which a process is unable to interact with its environment. Inaction can be used to describe deadlock.

**Successful termination:** In LOTOS exit is a nullary operator. It is equivalent to the following behaviour: $\delta$. stop, this sequential composition is an interaction with the special successful termination gate $\delta$, which ever appears explicitly in LOTOS program, followed by a stop operator (Fig. 2).

**Action prefix:**; The semantics of action prefix behaviour expression $B$ is: $M\text{-}\text{net}(G; B) = M\text{-}\text{net}(G); M\text{-}\text{net}(B)$ where $M\text{-}\text{net}(G)$ is given in (Fig. 2).

Choice $M\text{-}\text{net}(B_1 \parallel B_2) = M\text{-}\text{net}(B_1); M\text{-}\text{net}(B_2)$.

**Parallel composition:** LOTOS has three kinds of parallel operators (Table 1):

- General case $B_1 \mid [(G_1, \ldots, G_j) \cup \{\delta\}] \mid B_2$, where $\{G_1, \ldots, G_j\}$, a set of user-defined gates called synchronization gates of $B_1$ and $B_2$.
- Pure interleaving $B_1 \parallel [G] \parallel B_2$ when the set of synchronization gates is only $\delta$.
- Full synchronization $B_1 \parallel [G] \parallel B_2$, when the set of synchronization gates is the set of all gates appearing in both behaviour expressions including $\delta$.

The $M\text{-}\text{nets}$ semantics of parallel operators is carried out in two stages: Concurrency is expressed applying the parallel operator of $M\text{-}\text{nets}$ algebra ($\parallel$).
Synchronization and communication LOTOS are expressed by coupling of all the committed transitions in a same event. Two transitions \( t_1 \) and \( t_2 \) belonging respectively to M-nets \( B_1 \) and \( B_2 \) must synchronize through \( \text{sy}_m \), if they have in their respective labels the same action gate symbol belonging to the set of synchronization gates of specified operator, either \( (G_1, \ldots, G_i) \) for the first case and \( (G) \) for the second.

Thus, the semantics of this three operators is:

\[
\text{M-net} (B_1 \parallel \text{B}_2) = (\text{M-net} (B_1)) \parallel (\text{M-net} (B_2))
\]

\[
\text{M-net} (\text{B}_1 | | \text{B}_2) = (\text{M-net} (\text{B}_1) | | \text{M-net} (\text{B}_2)) \text{sy}_m \{ \delta \}
\]

\[
\text{M-net} (\text{B}_1 || \text{B}_2) = (\text{M-net} (\text{B}_1)) || (\text{M-net} (\text{B}_2))
\]

\[
\text{M-net} \{G_1, \ldots, G_i\} = (\text{M-net} \{G_1, \ldots, G_i\}) \text{sy}_m \{ \delta \}
\]

\[
\text{with } (G_1, \ldots, G) = (\text{gatelist } i)
\]

**Sequential composition**

\[
\text{M - net}(B_1 \gg B_2) = \text{M - net}(B_1) \cdot \text{M - net}(B_2)
\]

Hiding The operator hide ... in allows one to transform some observable actions of a process into unobservable ones. The M-nets semantics for the hiding operator consist of a renaming of all hidden gates by \( i \) (unobservable action) (Benzaken, 1998) over which no more interactions are possible.

\[
\text{M-net} \{h\text{ide} G_1, \ldots, G_i \text{ in } B\} = \text{M-net} (B) \text{ where } G_1, \ldots, G_i \text{ are renamed by } i
\]

**Disabling**: \( B_i \gg B \) in almost any OSI connection oriented protocol or service it is the case that the 'normal' course of action can be disrupted at any point in time by events signalling disconnection or abortion of a connection. This has led to the definition in basic LOTOS of an application generated operator namely the disabling operator. To illustrate such a disruption, we use a particularity M-net called M-net (TAbort) which contains a special kind of transition namely TAbort with an arbitrary (according to the whole of disrupted M-net places) number of entry-places and one exit-place. This transition is able to take into account this aborting by eliminating all token places of the disrupted behaviour net.

\[
M'(p) = 0 \text{ and } M(p) = 0
\]

The semantics of disabling is expressed by the following scoping:

\[
M(T\text{ Abort}) | M' \text{ with } \forall p \in t:
\]

**CONCLUSIONS**

Through the M-nets Algebra, a height level metalanguage and among simplest, we have presented a compositional semantics of a basic LOTOS specification. We have extensively made use of the modularity features of the M-net calculus and established thus a fully compositional model.

In this study we have only treated a simplified version of the language called basic LOTOS, while full LOTOS or fully LOTOS includes data structures that are derived from abstract data type language ACT ONE. The M-net formalism is insufficient for data type specification and another class of height level Petri-boxes: A-nets allows such a specification.

The tool of verification and simulation for a composed M-nets is the PEP (Programming Environment based on Petri-nets) system, its an interactive system allowing a visualization of some by step executions.

**REFERENCES**


